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Implementation of different wavelet transforms and threshold combinations for ECG De-noising

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Abstract: An Electro Cardiogram is the observation and recording of electrical information in the heart. Technological developments in the medical industry and non-aggressive monitoring of critical biological functions is an important need to provide appropriate care to patients and leads to their improved health. ECG signal analysis has been in use for a long time for cardiac problems. Technological advancements made the ECG observation quite easy but quite often, they get corrupted by different type of noises. Hence De-noising of ECG signal has gained a lot of importance. This paper deals with de-noising of three majorly encountered ECG disturbances viz. Power Line Interference, Wide Band Stochastic noise (EMG noise) and Base Line Wander noise. The De-noising is performed using various wavelet Transform techniques applying different types of threshold functions. Performance is measured using SNR and MSE and optimized combinations of Wavelet with a Threshold functions for different noises are suggested. The analysis is also done on real ECG signals obtained from Physionet medical database.

Keywords: Electro Cardiogram (ECG), Power Line interference, Electromyography (EMG) noise, Base line wander noise, Wavelet Transform, Signal to Noise ratio (SNR), Mean Square Error (MSE), Physionet.

I. INTRODUCTION

The Electrical activity of the heart is described by Electro Cardiogram, which is decomposed in characteristic components namely P, Q, R, S and waves.The rare cardiac events, anomalies like arrhythmias can be detected, predicted and monitored using ECG. The major concern of biomedical signal processing is need for reliable techniques to exclude the major distortions like noise contamination, artifacts and interference from other signals.

The non stationary behavior of ECG signal gives a tough challenge to denoise it. There are many approaches in the literature developed so far for the task of denoising. There are a no of approaches in ECG denoising like Linear Filters, Adaptive Filters and Kalman Filters, but all of them have their own limitations. The limitations include poor SNR, MSE and complexity.

Research results proved that WTs can be an effective tool in handling the non-stationary nature of signals. Donoho et al combined wavelet de noising and threshold estimations which laid a path to use the technique in ECG de-noising. Many hybrid algorithms came up combining Wavelet with different other techniques giving out proven results.

In this paper by combining Wavelet filtering with Threshold, some of the wavelet coefficients are removed, hence smoothing out the signal. Donoho's method has been the inspiration for de noising and works well for a wide class of one-dimensional and two-dimensional signals. The noise content of the signal is reduced, effectively, under the non-stationary environment.

In this paper a wide variety combinations of Wavelets and Thresholds are deployed and the appreciable combinations for a particular noise are suggested. The most disturbing noises for ECG like Power Line Interference, EMG noise and Base line drift are removed using the techniques.

The process of de-noising include, applying Wavelet Transform to the signal, shrinking the coefficients using various thresholds and finally taking the inverse wavelet transform. SNR and MSE will be the performance evaluators.

In the further sections, this paper discusses about Discrete Wavelet Transforms, Threshold techniques, Implementation and the results obtained.

II. WAVELET TRANSFORMS

A wavelet is a small wave whose energy is concentrated in time, which is useful for the analysis of transient, non-stationary or time-varying phenomena. Such a wave can be expressed and analyzed as a linear decomposition of the sums and products of the coefficient and function.

For Example, any signal x(n) decomposition can be done by simultaneously passing it through a series of high and low pass filters with impulse responses as h(n) and g(n) respectively. The outputs of high and low pass filters are named as detailed and approximate coefficients respectively.

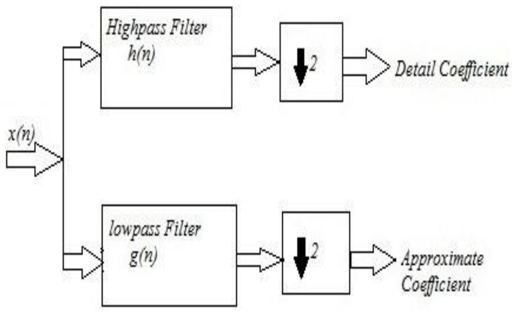

Fig. 1. Wavelet Decompostion

In the decomposition process, the down-sampling by 2 divides the input frequency by 2, thus doubling the

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Vol. 3, Issue 7, July 2015

frequency resolution further making the time resolution half. Increasing the levels of decomposition, which is user defined and application specific, will increase the frequency resolution further. Typically 3 to 5 levels are cascaded.

In the wavelet transform, the original signal (1-D, 2-D, 3-D) is transformed using predefined wavelets. The wavelets are orthogonal, orthonormal, or biorthogonal, scalar or multiwavelets. In discrete case, the wavelet transform is modified to a filter bank tree using the Decomposition/ reconstruction given in Fig.2.

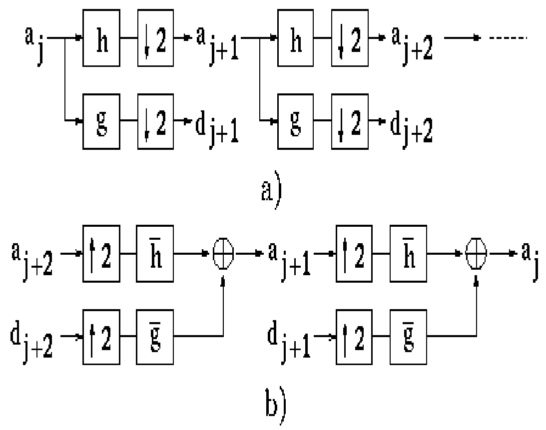

Fig. 2 DWT and IDWT

The wavelet transform de-noising is based on the statement that most energy of a signal is concentrated in few coefficients whereas noise is spread over a large number of coefficients. The shrinkage step involves implementing a nonlinear threshold over these coefficients to retain the larger magnitude (signal) coefficients and nullifying the smaller magnitudes (noise).

III. THRESHOLD ESTIMATION

Thresholds are usually applied only on the detailed coefficients as approximation coefficients contain low frequency components which are least affected by noise. The magnitude of coefficients is compared to a threshold level, denoted by 'λ' and an optimized value of λ is estimated. To estimate the threshold λ, we need to calculate the noise level σ. Among many methods for estimating value of σ, a popular one proposed by Donoho and Jhonstone is based on the detail coefficients of the last level calculated with the help of median absolute deviation (MAD) as per the following formulae:

$$\sigma = (|x - x'|)/\ 0.6745 \quad (1)$$

Where, 0.6745 is the scaling factor for a normally distributed data. Further, to estimate the threshold level 'λ', a universal threshold was used which is a function of noise level 'σ' and length of signal ' k', given as:

$$\lambda = \sigma\ \sqrt{2}\ \log(k) \qquad (2)$$

This shrinkage step is also referred as *wavelet thresholding*.

The thresholds implemented in this paper are Rigrsure, Heursure, Sqtwolog and Minimaxi under the cases of both soft and hard thresholding. Each and every threshold in their own case of hard and soft have their own set of advantages for a particular noise when used with a particular combination of wavelet. The various combinations of Thresholds with wavelets are performed and tabulated in the results.

A. Sqtwolog Threshold: This is also known as fixed threshold or global thresholding method and it is calculated as:

$$\lambda = \sigma\ \sqrt{2}\ \log\ (k)\ (3)$$

Where 'λ' is the threshold level, 'σ' is the noise level and 'k' is the length of the signal.

B. Rigrsure Threshold: Steins unbiased risk estimator (SURE) or rigrsure is an adaptive thresholding method which is proposed by Donoho and Jonstone .

C. Heursure Threshold: Heursure threshold is a combination of SURE and global thresholding method. If the signal-to noise ratio of the signal is very small, then the SURE method estimation will account for more noises. In this kind of situation, the fixed form threshold is selected by means of global thresholding method.

D. Minimaxi Minimax: Threshold is also used fixed threshold and it yields minmax performance for Mean Square Error (MSE) against an ideal procedures

E. Hard Thresholding:

$$S\ \lambda(d) = d.\ (abs(d) > \lambda)$$

F. Soft Thresholding

$$S\ \lambda(d) = \{$$
$$(d)(|d| - \lambda);\ |d| \geq \lambda 0;\ |d| < \lambda$$

IV. METHODOLOGY

An experimental setup is made and a broad comparison of various denoising techniques for variety combinations of wavelets and thresholds is made for each type of noise in ECG signal (viz. baseline drift noise, EMG noise and Powerline interference noise). The experimental setup is as follows.

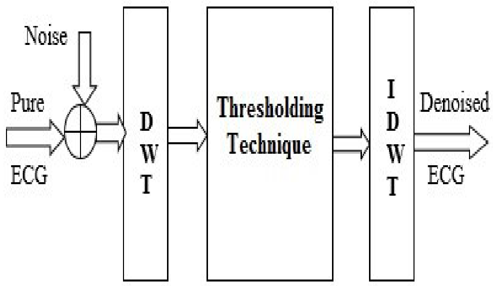

Fig. 3 Experimental Setup

A. Removal of EMG/wideband stochastic noise

The whole process can be summarized in the following steps:-

Step1: Decomposition of the noisy ECG signal is done into the wavelet coefficients using the wavelet decomposition tree. Any of the wavelet can be chosen from the wavelet family for this purpose.

Step 2: From the obtained wavelet coefficients the noise variance is estimated and thus threshold level λ is estimated using the universal threshold formulae as discussed earlier.

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Step 3: Then the different thresholding schemes are implemented and finally modified coefficients are reconstructed using the IDWT.

B. Removal of Baseline Drift

Among the many proposed algorithms for removal of baseline drift noise, in this paper the adopted algorithm is based on wavelet approach for baseline wander suppression. This noise constitutes a frequency band of 0-0.5 Hz and thus for the purpose of denoising following steps are performed:-

Step1: **S**ignal is decomposed in a way that the final level of the approximation coefficients represents a frequency band of 0-0.5 Hz.

Step2: The noise variance is then estimated from this very level of the decomposed coefficients. For a 1 KHz signal, at a scale of 28, the approximation coefficient represents a frequency band of 0-0.5 Hz.

Step3: These coefficients are modified in accordance with the thresholding scheme.

C. Removal of Power Line Interference

The power-line signal is a narrow-band signal. For removing the PLI, whole process can be summarized in the following steps:-

Step1: The noise is estimated using the *2nd level wavelet coefficients* that correspond to the frequency band of this signal (50/60 Hz).

Step2: Once the signal noise estimation is done, the threshold value is estimated and further the detailed coefficients are modified accordingly.

Step3: The updated wavelet coefficients are then reconstructed to give the denoised signal

V. RESULTS

The implementation is done on various types of noises using various wavelets and thresholds to finalize the best wavelet and threshold combination for a particular type of noise. For generating power line interference (PLI) a power line signal of frequency 60Hz is added to the original signal so that the input SNR (PLI)=8.0437 dB is obtained as in fig. 5(a). For input ECG with EMG noise as in Fig 6(a), white noise (20-250 Hz broadband with 10% of maximum amplitude) is superimposed over pure ECG signal so as to obtain an SNR (EMG) of 6.1817dB. For baseline wandered noisy ECG as in Fig. 4(b), low frequency (below 0.6 Hz) sinusoids are added to obtain the SNR of the input signal as SNR (BW) = –2.4526 db.

The performance is measured on the basis of the mean square Error (MSE) in accordance with the following formulae:

$$MSE = \frac{1}{N}\sum_{i=1}^{N}(x(i) - dn(i))^2,$$

And Signal to Noise ratio (SNR) of the input (noisy) ECG and SNR of output (denoised) ECG.

$$SNR_{input} = 10\log_{10}\left[\frac{\sum_{i=1}^{N} x(i)^2}{\sum_{i=1}^{N}(x(i)-n(i))^2}\right]$$

$$SNR_{output} = 10\log_{10}\left[\frac{\sum_{i=1}^{N} x(i)^2}{\sum_{i=1}^{N}(x(i)-dn(i))^2}\right]$$

Where, *x (i)* is the pure ECG signal, *n(i)* is noisy ECG, *dn(i)* is denoised ECG and *N* is the total number of samples.

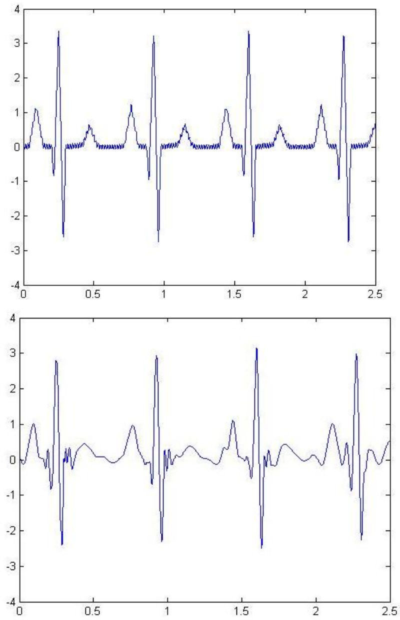


Fig.4 (a) Power-Line affected ECG (b) Power-Line corrected ECG Using rbio6.8 wavelet and minimaxi hard threshold

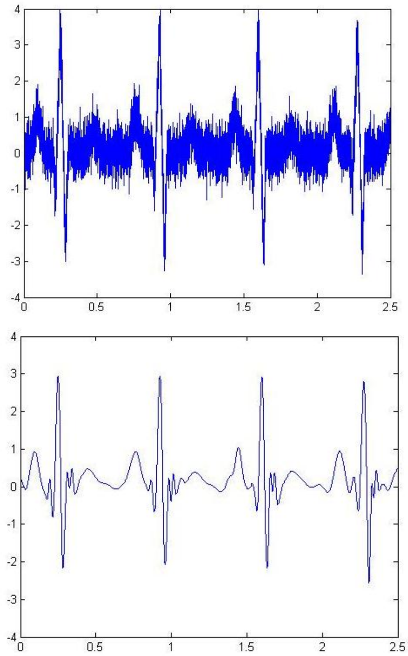
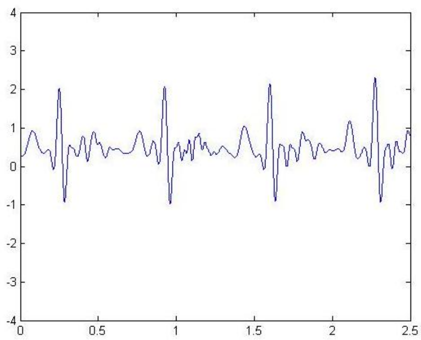


Fig. 5 (a) EMG affected ECG (b) EMG Corrected ECG using coif5 wavelet and sqtwolog threshold.



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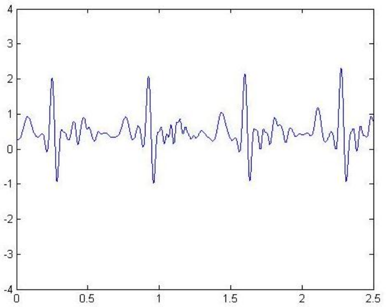

Fig. 6(a) Baseline affected signal, 5(b) Baseline Corrected signal using db45 wavelet and minimaxi threshold

Table 1: SNR in denoised ECG in case of PowerLineInterference (Input SNR = 21.31dB)

	RIGRSURE		HEURSURE		SQTWOLOG		MINIMAXI	
Thresholds/Wavets	SOFT	HARD	SOFT	HARD	SOFT	HARD	SOFT	HARD
bior3.9	40.46	51.51	39.33	34.75	5.53	29.6	9.45	20
bior4.4	28.24	44.81	28.6	44.69	6.51	27.6	9.47	32.73
bior5.5	25.4	46.1	25.4	46.1	4.75	49.22	7.97	33.96
bior6.8	33.36	45.41	33.42	45.22	8.38	37.3	11.86	69.49
bior1.1	14.81	14.81	14.21	15.27	4.06	29.99	7.75	18.58
bior1.3	16.74	15.97	16.74	15.97	6.72	15.11	11.74	14.48
bior1.5	21.58	16.56	21.58	16.54	8.16	13.46	13.97	13.26
bior2.2	27.58	35.34	25.76	31.27	8.42	21.11	10.82	21.11
bior2.4	27.2	29.78	27.62	32.41	8.22	29.61	10.89	24.15
bior2.6	26.45	25.31	25.97	25.31	8.36	22.8	11.12	26.4
bior2.8	24.46	28.55	24.46	28.55	8.34	24.97	11.08	24.82
bior3.1	61.34	39.9	61.34	39.9	-1.11	9.95	1.89	25.49
bior3.3	34.24	31.59	34.21	31.59	5.07	31.35	8.79	21.37
bior3.5	30.29	32.09	30.29	32.09	6.44	11.08	10.87	22.39
bior3.7	28.92	36.56	28.05	33.34	5.94	18.17	10.42	17.25
rbio1.1	14.81	14.81	14.21	15.27	4.06	29.99	7.75	18.58
rbio1.3	20.05	61.4	21.14	52.17	3.11	40.75	6.52	13.64
rbio1.5	43.94	34.83	43.94	34.83	3.2	9.15	6.68	20.1
rbio2.2	19.9	25.02	19.92	25.02	1.57	10.51	3.57	11.19
rbio2.4	15.1	18.27	15.08	18.22	2.74	18.02	5.35	17.87
rbio2.6	19.41	25.44	19.41	25.44	3.85	27.69	6.87	25.82
rbio2.8	23.48	44.5	23.48	44.5	4.71	32.08	8.06	38.03
rbio3.1	24.34	15.56	24.34	15.56	-8.2	3.25	-3.62	1.16
rbio3.3	29.43	22	29.43	22	8.6	12.17	22.78	4.86
rbio3.5	19.89	39.69	19.89	39.69	7.01	9.65	15.48	4.32
rbio3.7	24.91	31.09	24.91	31.09	5.51	11.33	11.04	11.38
rbio3.9	24.97	34.59	24.97	34.59	4.38	16.19	8.76	13.66
rbio4.4	17.97	24.23	18.17	24.21	5.27	18.72	7.82	20.38
rbio5.5	26.58	39.1	26.5	39.1	8.6	51.62	11.62	26.46
rbio6.8	26.65	33.16	26.65	33.16	7.55	31.88	11.04	31.11
dmey	28.73	30.26	32.59	30.25	8.06	23.72	10.89	23.57
coif1	19.42	31.17	19.43	31.12	4.22	13.52	6.31	15.42
coif2	19.62	24.4	19.62	24.4	6.13	22.17	8.72	24.68
coif3	24.55	36.46	24.55	36.46	7.49	22.67	10.33	27.85
coif4	29.11	66.34	29.11	66.34	8.01	33.37	11	29.57
coif5	32.64	39.12	32.64	39.12	8.36	35.1	11.39	29.75
sym8	38.44	38.01	39.04	38.19	8.49	39.92	12.14	34.22
sym16	42.25	35.66	42.25	35.66	9.85	20.06	14.42	20.93
db1 or haar	14.81	14.81	14.21	15.27	4.03	29.99	7.75	18.58
DB4	44.87	30.8436	44.87	30.8436	6.32	15.7489	8.14	14.87
db16	38.7	30.6	38.61	30.68	3.71	14.29	6.82	29.19
db45	27.2	30.25	27.2	30.25	5.92	29.44	8.81	21.71
db30	41.85	26.05	41.85	26.05	7.44	35.63	11.2	21.02

Table 2: SNR in denoised ECG in case of EMG Noise (Input SNR =11.06)

	RIGRSURE		HEURSURE		SQTWOLOG		MINIMAXI	
Thresholds/Wavets	SOFT	HARD	SOFT	HARD	SOFT	HARD	SOFT	HARD
bior3.9	36.03	47.05	37.12	45.19	5.16	28.12	8.95	20.42
bior4.4	23.74	39.68	24.18	39.77	5.05	20.01	7.8	24.04
bior5.5	30.93	28.8	30.93	28.8	4.18	11.61	7.11	30.98
bior6.8	24.03	25.56	25.05	25.54	8.41	29.62	11.99	48.95
bior1.1	12.03	11.66	11.42	11.08	3.28	20.84	6.52	47.99
bior1.3	19.01	15.29	19.01	15.29	7.09	14.21	12.36	14.36
bior1.5	19.03	14.75	19.03	14.75	7.13	15.78	12.05	13.5
bior2.2	22.91	57.26	23.38	57.26	7.24	17.33	9.42	18.87
bior2.4	23.87	29.37	23.87	29.37	9.06	29.34	11.94	25.69
bior2.6	22.35	27.33	22.11	27.33	7.65	24.78	10.38	24.85
bior2.8	20.93	24.05	21.02	24.7	7.45	21.04	9.94	20.86
bior3.1	13.27	16.06	13.27	16.06	36.65	30.82	14.97	3.55
bior3.3	33.05	33.09	33.05	33.09	4.91	12.68	8.65	17.8
bior3.5	25.73	19.08	25.73	19.08	6.21	13.99	10.97	15.72
bior3.7	25.25	19.69	25.25	19.69	6.21	17.19	10.57	22.1
rbio1.1	12.91	13.69	12.33	13.05	3.07	19.4	6.33	26.92
rbio1.3	51.72	21.52	51.48	21.47	3.56	31.66	6.92	58.78
rbio1.5	22.25	16.11	22.25	16.11	3.33	13.96	7.41	18.94
rbio2.2	15.46	30.57	18.47	30.57	1.16	5.42	3.07	12.48
rbio2.4	16.59	28.4	16.57	28.53	1.46	13.8	3.99	17.97
rbio2.6	19.61	29.02	19.62	29.02	2.55	9.93	5.32	20.18
rbio2.8	23.69	35.11	23.69	35.11	2.17	11.21	5.04	33.98
rbio3.1	11.7	5.47	11.7	5.47	-7.87	-3.16	-2.49	-0.65
rbio3.3	21.56	26.15	21.56	26.15	9.01	11.02	28.45	5.05
rbio3.5	18.2	37.12	18.2	37.12	8.63	7.85	21.45	6.22
rbio3.7	24.12	22.99	24.12	22.99	5.69	10.43	12.14	7.36
rbio3.9	31.33	29.47	31.33	29.47	4.14	17.31	8.34	13.67
rbio4.4	16.48	20.64	16.52	20.65	3.21	20.35	5.96	23.61
rbio5.5	27.18	28.2	29.99	28.2	14.13	17.91	19.47	23.59
rbio6.8	19.19	20.63	19.19	20.63	6.08	29.2	9.12	28.71
dmey	24.58	55.98	26.67	55.9	7.31	22.8	9.85	20.45
coif1	18.14	20.98	18.16	20.96	3.22	14.43	5.67	16.75
coif2	21.82	27.41	21.82	27.41	7.55	33.84	10.47	23.98
coif3	20.64	24.55	20.64	24.55	7.15	26.56	9.89	29.53
coif4	20.17	27.28	20.17	27.28	5.38	18.66	8.13	23.31
coif5	41.05	26.01	41.05	26.01	8.8	59.87	11.95	35.59
sym8	23.61	27.67	23.75	27.66	5.93	25.95	8.71	31.74
sym16	34.64	27.78	34.64	27.78	9.34	21.77	13.8	18.57
DB1 or haar	28.35	20.98	25.68	22.43	5.57	23.27	9.59	14.15
DB4	24.38	37.35	24.38	37.35	5.96	12.7	7.87	14.44
db16	54.81	23.26	54.81	23.26	3.65	14.03	6.55	21.16
db45	22.82	27.01	22.9	27.78	5.28	27.43	8.49	44.09

Table 3:SNR in denoised ECG in case of Base Line Wander Noise (Input SNR =8.68dB)

	RIGRSURE		HEURSURE		SQTWOLOG		MINIMAXI	
esholds/Wa	SOFT	HARD	SOFT	HARD	SOFT	HARD	SOFT	HARD
bior3.9	8.0129	8.2631	8.0129	8.2631	15.9919	6.2267	30.4464	6.3946
bior4.4	10.1169	8.6763	10.0675	8.6746	16.111	11.1031	39.5602	9.5255
bior5.5	10.1478	8.4148	10.1478	8.4148	11.6558	9.8969	21.7285	9.8183
bior6.8	9.5525	9.0026	9.5225	9.0026	25.4284	8.6818	22.0204	9.3181
bior1.1	14.6984	14.7855	15.087	14.1194	11.624	9.5643	27.1157	6.3172
bior1.3	13.1876	13.6374	13.187	13.6374	20.5021	5.3159	19.3086	5.1068
bior1.5	10.7905	12.0195	10.7905	12.0195	32.4518	4.751	15.5691	4.6749
bior2.2	10.9859	10.2231	10.8571	10.1065	22.1488	13.1373	34.9326	12.5179
bior2.4	10.3648	9.585	10.2787	9.5855	23.0083	11.1316	28.117	11.0254
bior2.6	10.1589	10.0807	10.2287	10.0807	25.0945	10.4712	24.9389	10.3989
bior2.8	10.696	9.7269	10.696	9.7269	26.813	10.274	23.8394	10.3996
bior3.1	8.4516	8.064	8.4516	8.064	4.6101	23.9522	10.3309	9.5756
bior3.3	8.3697	8.0769	8.3697	8.0769	14.3859	7.8078	45.8913	6.864
bior3.5	8.2142	8.1191	8.2142	8.1191	19.2758	5.1577	22.4151	7.1338
bior3.7	8.0718	8.18	8.0718	8.18	19.2829	5.6271	22.666	6.807
rbio1.1	14.6984	14.7855	15.087	14.1197	11.6264	9.5643	27.1157	6.3172
rbio1.3	12.6114	8.6178	11.5142	8.7168	9.2488	8.5096	20.4289	5.8222
rbio1.5	8.6985	8.2358	8.6985	8.2358	9.4159	34.5262	20.6395	7.2089
rbio2.2	12.5601	8.6685	12.553	8.6685	6.097	23.3357	10.09	20.556
rbio2.4	13.7353	12.2151	13.7536	12.2352	7.6596	14.4572	13.234	13.1826
rbio2.6	10.9762	9.7596	10.7949	9.7596	9.3239	10.7164	17.2144	10.1733
rbio2.8	10.6956	9.0904	10.6956	9.0904	11.2554	8.974	22.439	8.8606
rbio3.1	8.9304	16.9004	8.9304	16.9004	-7.1452	0.1548	-1.9222	-1.1736
rbio3.3	7.8848	10.8042	7.8848	10.8042	38.6771	4.3546	10.9404	0.6508
rbio3.5	7.3322	9.8321	7.3322	9.8321	21.2707	2.5447	14.2722	0.2693
rbio3.7	7.6542	9.2773	7.6542	9.2773	14.8026	4.1668	22.9007	3.6463
rbio3.9	7.8219	9.6698	7.8219	9.6698	11.7377	6.0245	35.0045	5.0698
rbio4.4	11.9801	10.2766	11.9151	10.2789	12.5494	12.1896	21.2686	11.8471
rbio5.5	10.4947	9.0314	10.4827	9.0314	24.7485	9.6394	24.1544	9.4159
rbio6.8	10.2703	9.4672	10.2703	9.4672	19.3912	8.9365	27.9125	8.8739
dmey	9.5577	9.9379	9.2288	7.5457	33.4956	10.201	21.246	9.765
coif1	11.6943	7.8504	11.6937	7.8474	11.0631	15.0527	17.241	15.3289
coif2	11.4436	9.9064	11.4436	9.904	14.605	11.8285	26.3223	11.8101
coif3	10.5299	9.2215	10.5299	9.2215	19.8394	10.6188	31.7616	10.6267
coif4	9.8077	8.7422	9.8077	8.7422	24.8048	9.4933	24.843	10.1956
coif5	9.6836	8.5411	9.6836	8.5412	28.3761	9.6782	22.3862	10.0448
sym8	9.202	9.178	9.1758	9.1704	26.2078	8.2283	21.3954	8.9895
sym16	8.5038	8.0311	8.5038	8.0311	38.2878	7.2025	16.7397	7.013
db1 or haa	14.6984	14.7855	15.087	14.1194	11.6264	9.5643	27.1157	6.3172
DB4	8.7653	7.7978	8.7653	7.7978	17.0486	13.8173	28.6137	14.4262
db16	9.0724	7.7845	9.0724	7.7845	10.7548	15.4268	20.786	7.8725
db45	10.1861	9.4223	10.1861	9.4223	16.7862	9.5514	71.4447	7.0609

Table 4: MSE in denoised ECG in case ofPower Line interference Noise (MSE Noisy signal =0.000016)

	RIGRSURE		HEURSURE		SQTWOLOG		MINIMAXI	
Thresholds/Wavets	SOFT	HARD	SOFT	HARD	SOFT	HARD	SOFT	HARD
bior3.9	0.0002	0	0.0003	0.0007	0.619	0.0024	0.25	0.02
bior4.4	0.0033	0.0001	0.003	0.0001	0.4935	0.0038	0.2496	0.0012
bior5.5	0.0064	0.0001	0.0064	0.0001	0.7397	0	0.3523	0.0009
bior6.8	0.001	0.0001	0.001	0.0001	0.3206	0.0004	0.144	0
bior1.1	0.0729	0.073	0.0839	0.0656	0.8679	0.0022	0.3711	0.0306
bior1.3	0.0468	0.0558	0.0468	0.0558	0.4706	0.0681	0.1479	0.0787
bior1.5	0.0154	0.0488	0.0154	0.0488	0.3372	0.0995	0.0885	0.1043
bior2.2	0.0039	0.0006	0.0059	0.0016	0.3176	0.0171	0.1828	0.0171
bior2.4	0.0042	0.0023	0.00038	0.0013	0.3327	0.0027	0.1799	0.0085
bior2.6	0.005	0.0065	0.0056	0.0065	0.3223	0.0137	0.1707	0.0051
bior2.8	0.0079	0.0031	0.0079	0.0031	0.3239	0.007	0.1724	0.0073
bior3.1	0	0	0	0	0.2859	0.0223	0.1441	0.0006
bior3.3	0.0008	0.0015	0.0008	0.0015	0.6876	0.0016	0.2919	0.0161
bior3.5	0.0021	0.0014	0.0024	0.0014	0.5014	0.1722	0.181	0.0127
bior3.7	0.0028	0.0005	0.0035	0.001	0.5622	0.0337	0.2004	0.0417
rbio1.1	0.0729	0.073	0.0839	0.0656	0.8679	0.0022	0.3711	0.0306
rbio1.3	0.022	0	0.017	0	1.08	0	0.49	0.096
rbio1.5	0	0.001	0	0.001	1.059	0.269	0.474	0.022
rbio2.2	0.023	0.007	0.022	0.007	1.53	0.19	0.97	0.16
rbio2.4	0.068	0.033	0.069	0.033	1.175	0.035	0.645	0.036
rbio2.6	0.253	0.063	0.253	0.063	9.106	0.038	4.54	0.058
rbio2.8	0.099	0.001	0.099	0.001	7.478	0.014	3.455	0.003
rbio3.1	0	0	0	0	15	1	5	2
rbio3.3	0.0025	0.014	0.0025	0.014	0.305	0.1339	0.0117	0.7223
rbio3.5	0.0227	0.0002	0.0227	0.0002	0.4401	0.2393	0.0625	0.8177
rbio3.7	0.0071	0.0017	0.0071	0.0017	0.6206	0.1625	0.1739	0.1609
rbio3.9	0.007	0.0008	0.007	0.0008	0.8061	0.0531	0.2939	0.0951
rbio4.4	0.0353	0.0083	0.0337	0.0084	0.656	0.0297	0.3647	0.0203
rbio5.5	0.0049	0.0003	0.0049	0.0003	0.3051	0	0.1522	0.005
rbio6.8	0.0048	0.0011	0.0048	0.0011	0.3882	0.0014	0.174	0.0017
dmey	0.003	0.0021	0.0012	0.0021	0.3456	0.0094	0.18	0.0097
coif1	0.0252	0.0017	0.0252	0.0017	0.8367	0.0982	0.5166	0.0634
coif2	0.0241	0.008	0.0241	0.008	0.5385	0.0134	0.2965	0.0075
coif3	0.0077	0.0005	0.0077	0.0005	0.3938	0.0119	0.2048	0.0036
coif4	0.0027	0	0.0027	0	0.3494	0.001	0.1755	0.0024
coif5	0.0012	0.0003	0.0012	0.0003	0.322	0.0007	0.1606	0.0023
sym8	0.0003	0.0003	0.0003	0.0003	0.3126	0.0002	0.1349	0.0008
sym16	0.0001	0.0006	0.0001	0.0006	0.2287	0.0218	0.0798	0.0179
DB1 or haar	0.0729	0.073	0.0839	0.0656	0.8679	0.0022	0.3711	0.0306
DB4	0.0001	0.0018	0.0001	0.0018	0.516	0.0589	0.3392	0.0721
db16	0.0003	0.0019	0.0003	0.0019	0.9411	0.0824	0.4593	0.0027
db45	0.0042	0.0021	0.0042	0.0021	0.5658	0.0025	0.2904	0.0149

Table 5: MSE in denoised ECG in case of EMG Noise (MSE Noisy signal =0.00075)

	RIGRSURE		HEURSURE		SQTWOLOG		MINIMAXI	
Thresholds/Wavets	SOFT	HARD	SOFT	HARD	SOFT	HARD	SOFT	HARD
bior3.9	0.0342	0.2215	0.0178	0.035	0.5431	0.0196	0.1893	0.0547
bior4.4	0.0018	0.0321	0.0022	0.0322	0.7113	0.0055	0.3581	0.0038
bior5.5	0.0101	0.0021	0.0101	0.0021	0.788	0.1327	0.4357	0.0073
bior6.8	0.0069	0.0026	0.0069	0.0026	0.3651	0.0004	0.175	0
bior1.1	0.0247	0.0284	0.027	0.0309	0.1047	0.0019	0.0516	0.0004
bior1.3	0.0157	0.0408	0.0157	0.0408	0.4685	0.0688	0.1466	0.0676
bior1.5	0.0276	0.0544	0.0276	0.0544	0.4341	0.0563	0.1406	0.0603
bior2.2	0.011	0.0002	0.0099	0.0002	0.3785	0.0294	0.2263	0.0294
bior2.4	0.0048	0.0288	0.0043	0.0288	0.5051	0.0274	0.2903	0.0278
bior2.6	0.0437	0.097	0.0402	0.0352	0.4733	0.0183	0.2669	0.0291
bior2.8	0.0258	0.0031	0.0257	0.0031	0.5759	0.0383	0.3363	0.0322
bior3.1	1.463	1.299	1.794	2.275	0.063	2.372	0.049	1.463
bior3.3	0.0011	0.0005	0.0011	0.0006	0.8063	0.1868	0.4255	0.0002
bior3.5	0.0007	0.01515	0.0007	0.0115	0.6027	0.1052	0.2446	0.005
bior3.7	0.0162	0.035	0.0171	0.0459	0.3966	0.1016	0.1214	0.0533
rbio1.1	0.0336	0.0359	0.0439	0.0332	0.8142	0.0003	0.3146	0.0368
rbio1.3	0.0037	0.002	0.0037	0.002	0.824	0.0164	0.3164	0.0856
rbio1.5	0.001	0	0.001	0	1.262	0.314	0.551	0.072
rbio2.2	0.005	0.029	0.005	0.029	1.203	0.118	0.739	0.098
rbio2.4	0.045	0.025	0.046	0.025	1.493	0.427	0.853	0.042
rbio2.6	0.013	0.003	0.013	0.003	1.149	0.008	0.587	0.011
rbio2.8	0.173	0.054	0.173	0.054	8.397	0.02	3.97	0.001
rbio3.1	0	0	0	0	0.0012	0.0004	0.0003	0.0003
rbio3.3	0.057	0.002	0.057	0.002	0.338	1.21	0.009	0.676
rbio3.5	0.0569	0.0001	0.0569	0.0001	0.4905	0.2862	0.0564	0.763
rbio3.7	0.0001	0.0281	0.0001	0.0281	0.6925	0.1587	0.1975	0.1862
rbio3.9	0.0148	0.0002	0.0148	0.0002	0.7916	0.0126	0.2734	0.1073
rbio4.4	0.0179	0.0041	0.0179	0.0041	0.7805	0.0463	0.4398	0.0294
rbio5.5	0.0178	0.0035	0.0186	0.0028	0.4523	0.0006	0.2206	0.0015
rbio6.8	0.0067	0.0006	0.0067	0.0006	0.7259	0.0052	0.3512	0.0001
dmey	0.0001	0.0064	0.0001	0.0064	0.3204	0.0078	0.1595	0.0005
coif1	0.0834	0.0504	0.0834	0.0504	0.9131	0.1057	0.5641	0.0859
coif2	0.0144	0.0018	0.0144	0.0018	0.7004	0.0237	0.3754	0.0189
coif3	0.0069	0.0002	0.0069	0.0002	0.7172	0.0077	0.3752	0.0079
coif4	0.0028	0	0.0028	0	0.4206	0.0044	0.2267	0.0108
coif5	0.0016	0.0017	0.0016	0.0017	0.4635	0.0059	0.224	0.0001
sym8	0.0096	0.0034	0.0094	0.0033	0.336	0.0018	0.1576	0
sym16	0.0037	0.0005	0.0037	0.0005	0.2327	0.0323	0.0826	0.0165
DB1 or haar	0.169	0.218	0.183	0.201	1.013	0.41	0.496	0.0006
DB4	0.0186	0.0004	0.0186	0.0004	0.5926	0.084	0.3942	0.1069
db16	0.0012	0.0045	0.0012	0.0045	0.8858	0.06	0.4441	0.0036
db45	0.007	0.0003	0.007	0.0003	0.5352	0.0006	0.2795	0.0028

Table 6: MSE in denoised ECG in case of BaseLinewander noise (MSE Noisy signal=0.000029)

	RIGRSURE		HEURSURE		SQTWOLOG		MINIMAXI	
esholds/Wa	SOFT	HARD	SOFT	HARD	SOFT	HARD	SOFT	HARD
bior3.9	0.3495	0.33	0.3495	0.33	0.0557	0.5274	0.002	0.5074
bior4.4	0.2153	0.3	0.2178	0.3001	0.0542	0.1716	0.0002	0.2467
bior5.5	0.2138	0.3186	0.2138	0.3186	0.1511	0.2265	0.0149	0.2307
bior6.8	0.2469	0.2783	0.2469	0.2783	0.0063	0.2996	0.0139	0.2588
bior1.1	0.075	0.0735	0.0686	0.0857	0.1521	0.2445	0.0043	0.2165
bior1.3	0.1062	0.0957	0.1062	0.0957	0.0197	0.6504	0.0259	0.6825
bior1.5	0.1844	0.1389	0.1844	0.1389	0.0013	0.7408	0.0614	0.7539
bior2.2	0.1763	0.2101	0.1816	0.2158	0.0135	0.1074	0.0007	0.1239
bior2.4	0.2034	0.2434	0.2075	0.2434	0.0111	0.1705	0.0034	0.1747
bior2.6	0.2133	0.2171	0.2099	0.2171	0.0068	0.1985	0.0071	0.2018
bior2.8	0.1884	0.2356	0.1884	0.2356	0.0046	0.2077	0.0091	0.2018
bior3.1	0.316	0.3455	0.316	0.345	0.7652	0.0089	0.205	0.2439
bior3.3	0.322	0.3444	0.322	0.3444	0.0806	0.3664	0.0001	0.4554
bior3.5	0.3337	0.3411	0.3337	0.3411	0.0261	0.6746	0.0127	0.428
bior3.7	0.3448	0.3363	0.3448	0.3363	0.0261	0.6055	0.012	0.4614
rbio1.1	0.075	0.0735	0.0686	0.0857	0.1521	0.2445	0.0043	0.5165
rbio1.3	0.1212	0.3041	0.1561	0.2972	0.263	0.3118	0.02	0.5788
rbio1.5	0.2985	0.3321	0.2985	0.3321	0.253	0.0008	0.0191	0.4206
rbio2.2	0.1227	0.3006	0.1229	0.3006	0.5434	0.0103	0.2167	0.0195
rbio2.4	0.0936	0.1328	0.0932	0.1322	0.3792	0.0793	0.105	0.1063
rbio2.6	0.1767	0.2338	0.1767	0.2338	0.2585	0.1876	0.042	0.2125
rbio2.8	0.1885	0.2727	0.1885	0.2727	0.1657	0.2801	0.0126	0.2876
rbio3.1	0	0	0	0	0.0011	0.0002	0.0003	0.0003
rbio3.3	0.036	0.0184	0.036	0.0184	0	0.0812	0.0178	0.1904
rbio3.5	0.0409	0.023	0.0409	0.023	0.0017	0.1231	0.0083	0.2079
rbio3.7	0.9796	0.2612	0.3796	0.2612	0.0732	0.8474	0.0113	0.9553
rbio3.9	0.3653	0.2387	0.3653	0.2387	0.1483	0.5525	0.0007	0.6883
rbio4.4	0.1402	0.2076	0.1423	0.2074	0.123	0.1336	0.0165	0.1446
rbio5.5	0.1974	0.2765	0.1979	0.2765	0.0074	0.2404	0.0085	0.253
rbio6.8	0.2079	0.2501	0.2079	0.2501	0.0254	0.2826	0.0036	0.2867
dmey	0.2449	0.3556	0.2642	0.3892	0.001	0.2112	0.0166	0.2335
coif1	0.1497	0.3629	0.1498	0.3631	0.1732	0.0691	0.0418	0.0648
coif2	0.1586	0.226	0.1586	0.226	0.0766	0.1452	0.0052	0.1458
coif3	0.1958	0.2646	0.1958	0.2646	0.023	0.1918	0.0015	0.1915
coif4	0.2312	0.2955	0.2312	0.2955	0.0078	0.2486	0.0073	0.2115
coif5	0.2379	0.3095	0.2379	0.3095	0.0028	0.2382	0.0128	0.2189
sym8	0.2658	0.2673	0.2674	0.2678	0.0053	0.3326	0.016	0.2791
sym16	0.3122	0.3481	0.3122	0.3481	0.0003	0.4212	0.0469	0.44
DB1 or haa	0.075	0.0735	0.0686	0.0857	0.1521	0.2445	0.0043	0.5165
DB4	0.2939	0.3673	0.2939	0.3673	0.0436	0.0918	0.003	0.0798
db16	0.2739	0.3684	0.2739	0.3684	0.1859	0.0634	0.0185	0.361
db45	0.2119	0.2527	0.2119	0.2527	0.0464	0.2453	0	0.4352
db30	0.3237	0.3885	0.3237	0.3885	0.0063	0.2518	0.019	0.4614

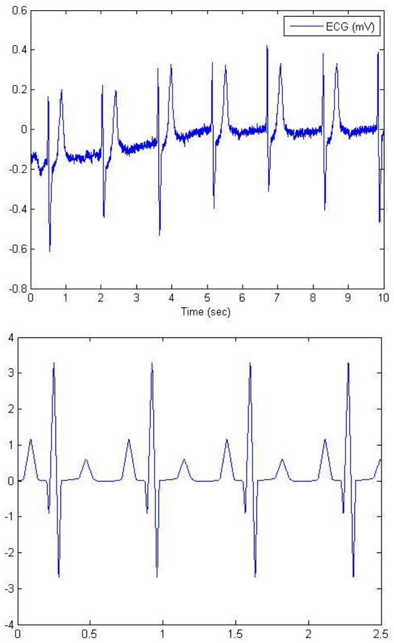

Fig. 7(a) Real time ECG signal from physionet database, 7(b) DE noised ECG signal using db4 wavelet and heursure soft threshold.

VI. CONCLUSION

The various types of wavelets and thresholds used in this paper are good in performance. But for a particular type of noise this paper comes out with a best combination of wavelet and threshold to be used.

Power Line Interference noise is best removed using the bior6.8 wavelet with a threshold combination of minimaxi hard threshold. The Baseline Wander noise can be removed effectively using the db45 threshold and minimaxi soft threshold. EMG noise is removed using coif5 wavelet with a threshold combination of sqtwolog hard threshold. Hence this paper comes out with best combinations of Wavelet and threshold for a particular noise. This paper can be improved by working on more types of noises and finding the solutions to them. Even study can be done on realizing a new type of wavelet and a new threshold which can be useful to denoise any kind of ECG Noise. In this paper Real ECG signal from Physionet database is taken and denoised using some of the wavelet and threshold combinations available.

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